

SE(ECS) sem-3 C-scheme Winter 2015

Date: 10/11/25

Time: 3 hour

Max. Marks: 80

Note: 1) Question 1 is compulsory.

2) Attempt any 3 questions from Question 2 to Question 6

3) Figures to the right indicate full marks.

Q1 Attempt All questions

A If $A = \begin{bmatrix} -1 & 0 & 0 \\ 2 & -3 & 0 \\ 1 & 4 & -2 \end{bmatrix}$ then find the eigen values of A^2 5

B Find Laplace transform of $f(t) = te^t \cos 2t$ 5

C Find the half range Sine Series for $f(x) = x$, where $x \in (-\pi, \pi)$ 5

D Determine the constant a, b, c, d if $f(z) = x^2 + 2axy + by^2 + i(cx^2 + 2dxy + y^2)$ is analytic. 5

Q2

A Using Green's theorem in a plane to evaluate the line integral 6

$$\oint_C (xy + y^2)dx + x^2 dy$$

Around the boundary of the region defined by $y=x^2$ and $y=x$

B Find the Eigen values and Eigen vectors of the matrix 6

$$A = \begin{bmatrix} 4 & 2 & -2 \\ -5 & 3 & 2 \\ -2 & 4 & 1 \end{bmatrix}$$

C Show that the function $v = e^x \sin y$ satisfies Laplace's equation, also find analytic function. 8

Q3

A Prove that $\vec{F} = (x^2 - yz)i + (y^2 - zx)j + (z^2 - xy)k$ is irrotational. 6

B Find the analytic function whose real part is $x^3 - 3xy^2 + 3x^2 - 3y^2 + 1$ 6

C Verify Cayley-Hamilton theorem for the matrix A and hence find A^{-1} and A^4 8

where $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$

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